

X-Ray Examples of SPNs⁶



Introduction

I investigated and compared commonly used stochastic models to predict if SPNs (Solitary Pulmonary Nodules) found in patients are malignant or benign.

Lung Cancer

Covariates Tested in each Model (Table 1):

Model	β ₀	Age	Smoker	Past Cancer	Diamet er	Spicula- tion	Upper Lobe	Family History	Calcific- ation	Clear Border	CEA	CYFRA 21-1	Satellite Lesion
Mayo 1	-6.827	0.039	0.792	1.339	0.127	1.041	0.7838						
Li-Wang	-4.496	0.070			0.676	0.736		1.267	-1.615	-1.408			
Wang	-4.294	0.035	1.029		0.633	2.027	2.673	0.974	-3.295	-1.631	0.221	0.200	-1.923

Model Comparison

One of the leading causes of cancer deaths since 1985⁴
Manifests in the appearance of solitary pulmonary nodules (SPNs) in the lungs, which can either be diagnosed as malignant (cancerous) or benign (non-cancerous)
Early detection of malignant SPNs can increase survival rate of cancer patients by 40%⁴

Mathematical models serve as tools for physicians to refrain from preforming unnecessary procedures in patients whose SPNs are most likely benign.

The Models

The Mayo Model 1¹: A model created in 1999 by the Mayo Clinic used clinical data to predict the outcome of SPNs

The Mayo Model 2²: The researchers at the Mayo Clinic studied the outcomes of SPNs predicted by physicians. A curve was created but no predictive model.

The Li-Wang Model³: In 2012, the Li-Wang model included family history of cancer as a predictor variable.

Sensitivity Analysis: Used to quantify the robustness

and uncertainty of model

	Model	Sensitivity	Specificity		
Table 2	Mayo 1	Not Provided	Not Provided		
Table Z	Mayo 2	Not Provided	Not Provided		
	Li-Wang	94.5%	70%		
	Wang	90.7%	81.2%		

*Sensitivity: Probability the model
model will produce a malignant
prediction when the SPN truly
is cancerous
*Specificity: Probability the model
will produce a true benign
prediction when the SPN truly is

Model Area Under the Curve

Cost Exploration : Used to assess the accessibility and monetary restrictions of the model

How accessible is the model?

The Mayo Model 1 is accessible online.

The Mayo Model 2 is the predictions of physicians without mathematical computations.

The Li-Wang Model and Wang Model are public, but must be computed manually.

Input:				Results				
Age	50	yr	•	incourts.				
				×	-1.64			
Smoker	Ourrent	or former (1)		Malig	16.27	%		
	Never sr	moker (0)		riobability				
Cancer	Cancer O Extrathoracic cancer more than 5 years prior (1)			Decimal Precision: 2 V				
	None (0))					_	
Nodule Diameter	11	mm	۲					
Spiculation	Yes (1)							
	O No (0)							
Upper Lobe	O Yes (1)							
	No (0)							
Formula	Notes	References	5					

An open source tool for Mayo Model 1 online at www.medscape.com.

What is the cost to obtain the data?

The Wang Model⁴: In 2013, Wang continued his research and added biomarker data and used an advanced statistical technique to develop the model.

All models used the same basic logistic regression model:

 $p = \frac{e^x}{1 + e^x}$

Where p is the probability a SPN is malignant, and e is the base of the natural logrithm.

The factors (independent covariates) that influence each model are listed in Table 1 with their respective β values. The β values can be interpreted as the weight each variable holds as a predictor of cancerous SPNs.

		(AUC)
Table 3	Mayo 1	0.798 ± 0.047
	Mayo 2	0.835 ± 0.033
	Li-Wang	0.874 ± 0.028
	Wang	0.935 ± 0.011

*Area Under the Characteristic Curve quantifies how accurate the model diagnosis SPNs. An AUC closer to 1 implies a stronger model.

Conclusion

Recommendation: Based on the sensitivity analysis and cost exploration, I recommend the Wang Model. Though the Mayo Model 1 is the most accessible, The Wang Model has the highest specificity and AUC. It is crucial to obtain true negatives when early detection can increase life expectancy. If the data collection is not possible for the Wang Model, I recommend the Li-Wang Model over The Mayo Model 1.

- The clinical information necessary for The Mayo Models 1 & 2, and the Li-Wang can be collected by easily by physicians.
- The Wang Model requires biomarker series tests and CT scans, which raises the cost of obtaining the data

Do physicians have the computational abilities?

The Wang Model requires a LASSO technique that requires a highly trained statistician or computer scientist.

Future Work: Though all of these models aid in the

diagnosis of SPNs, they are merely a tool to aid physicians. Further research needs to be done to make The Wang Model more accessible to all physicians and patients. More research needs to be done to find additional predictor variables that maximize the predictive power of stochastic models that predict the malignancy of SPNs.



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